

1. 2

$$\sin 25^\circ = \cos 65^\circ \text{ และ } \sin 45^\circ = \cos 45^\circ$$

$$\text{ดังนั้น } \sin 25^\circ + \sin 45^\circ = \cos 45^\circ + \cos 65^\circ$$

2. 4

$$\sin 30^\circ = \frac{1}{2} = 0.5, \quad \cos 45^\circ = \frac{\sqrt{2}}{2} = 0.7, \quad \tan 45^\circ = 1, \quad \sec 60^\circ = 2,$$

$$\csc 30^\circ = 2, \quad \tan 60^\circ = \sqrt{3} = 1.732, \quad \cos 60^\circ = \frac{1}{2} = 0.5$$

$$\text{ดังนั้น } \tan 60^\circ > \cos 60^\circ$$

3. 3

$$6 \tan^2 30^\circ - \frac{1}{4} \sec^2 45^\circ + \frac{5}{3} \sin^2 60^\circ = 6 \left(\frac{1}{\sqrt{3}} \right)^2 - \frac{1}{4} (\sqrt{2})^2 + \frac{5}{3} \left(\frac{\sqrt{3}}{2} \right)^2$$

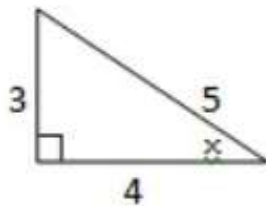
$$= 6 \left(\frac{1}{3} \right) - \frac{1}{4} (2) + \frac{5}{3} \left(\frac{3}{4} \right) = 2 - \frac{1}{2} + \frac{5}{4} = \frac{8-2+5}{4} = \frac{11}{4}$$

4. 2

$\hat{A} + \hat{B} = 90^\circ$ และ $\hat{A} : \hat{B} : \hat{C} = 1 : 2 : 3$ จะได้ $\hat{C} = 90^\circ$, $\hat{A} = 30^\circ$ และ $\hat{B} = 60^\circ$

$$(\cos B + \sin A)^2 = (\cos 60^\circ + \sin 30^\circ)^2 = \left(\frac{1}{2} + \frac{1}{2}\right)^2 = 1$$

5. 3



$$3 \cos x = 4 \sin x$$

$$\frac{\sin x}{\cos x} = \frac{3}{4}$$

$$\tan x = \frac{3}{4}$$

$$\cos x = \frac{4}{5} \text{ และ } \sin x = \frac{3}{5}$$

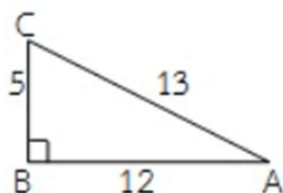
$$\sec x + \csc x = \frac{5}{4} + \frac{5}{3} = \frac{15 + 20}{12} = \frac{35}{12}$$

6. 1

$$\sin 20^\circ = 0.342 = \frac{342}{1,000}$$

$$\sec 70^\circ + \csc 20^\circ = \csc 20^\circ + \csc 20^\circ = 2 \csc 20^\circ = \frac{1000}{171}$$

7. 1



$$65 \sin A - 26 \cos A = 65 \left(\frac{5}{13} \right) - 26 \left(\frac{12}{13} \right) = 25 - 24 = 1$$

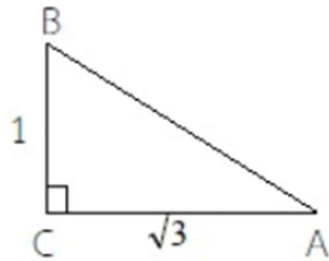
8. 2

$$\cos^2 A - \sin^2 A = \frac{1}{2} \rightarrow \cos^2 A - (1 - \cos^2 A) = \frac{1}{2} \rightarrow 2\cos^2 A - 1 = \frac{1}{2}$$

$$\rightarrow \cos^2 A = \frac{3}{4} \rightarrow \cos A = \frac{\sqrt{3}}{2} \rightarrow A = 30^\circ$$

$$\sec A + \tan A = \sec 30^\circ + \tan 30^\circ = \frac{2}{\sqrt{3}} + \frac{1}{\sqrt{3}} = \frac{3}{\sqrt{3}} = \sqrt{3}$$

9. 4



พื้นที่ของรูปสามเหลี่ยม $ABC = \frac{1}{2} \times \text{ความยาวของฐาน} \times \text{ความสูง}$

$$\frac{\sqrt{3}}{2} = \frac{1}{2} \times CA \times CB$$

$$CA \times CB = \sqrt{3}$$

จะได้ $CA = \sqrt{3}$, $CB = 1$ และ $\hat{A} = 30^\circ$, $\hat{B} = 60^\circ$

ดังนั้น ข้อ 4 ไม่ถูกต้อง เพราะ $\tan B = \tan 60^\circ = \sqrt{3}$

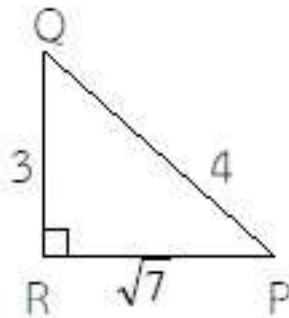
10. 3

$$B - A = \cos^2 45^\circ + \tan^2 60^\circ - \sin^2 60^\circ + \tan^2 30^\circ$$

$$= \left(\frac{\sqrt{2}}{2}\right)^2 + (\sqrt{3})^2 - \left(\frac{\sqrt{3}}{2}\right)^2 - \left(\frac{1}{\sqrt{3}}\right)^2 = \frac{1}{2} + 3 - \frac{3}{4} - \frac{1}{3}$$

$$= \frac{6 + 36 - 9 - 4}{12} = \frac{29}{12} = 2\frac{5}{12}$$

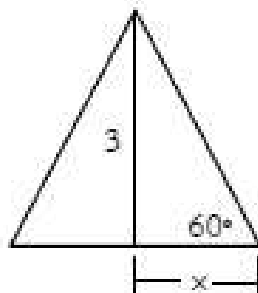
11. 2



$$\hat{P} + \hat{Q} = 90^\circ \text{ และ } \sin P = 0.75 = \frac{3}{4}$$

$$\frac{\sin Q + \cos P}{\tan Q} = \frac{\cos P + \cos P}{\tan Q} = \frac{2 \cos P}{\tan Q} = 2 \left(\frac{\sqrt{7}}{4} \right) \left(\frac{3}{\sqrt{7}} \right) = \frac{3}{2}$$

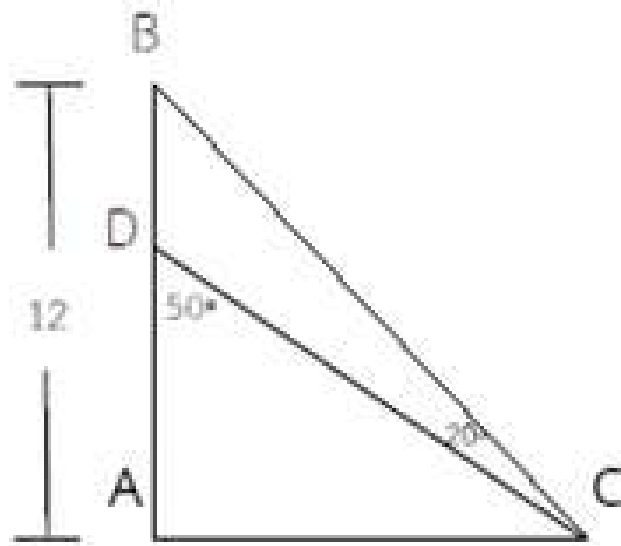
12. 1



$$\tan 60^\circ = \frac{3}{x} \rightarrow \sqrt{3} = \frac{3}{x} \rightarrow x = \sqrt{3}$$

$$\text{พื้นที่ของรูปสามเหลี่ยม} = \frac{1}{2} \times 2(\sqrt{3}) \times 3 = 3\sqrt{3} \text{ ตารางหน่วย}$$

13. 3



$$\tan 30^\circ = \frac{AC}{12} \rightarrow \frac{1}{\sqrt{3}} = \frac{AC}{12} \rightarrow AC = 4\sqrt{3}$$

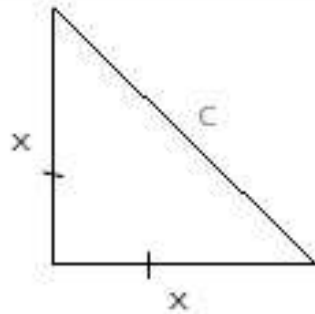
$$\text{พื้นที่ของรูปสามเหลี่ยม } ABC = \frac{1}{2} \times 4\sqrt{3} \times 12 = 24\sqrt{3}$$

14. 3

$$\text{จะได้ } CA = \sqrt{3}, CB = 1 \text{ และ } \hat{A} = 30^\circ, \hat{B} = 60^\circ$$

$$\text{ดังนั้น } \cos A = \cos 30^\circ = \frac{\sqrt{3}}{2}$$

15. 1



$$\text{จาก } c = \sqrt{2}x$$

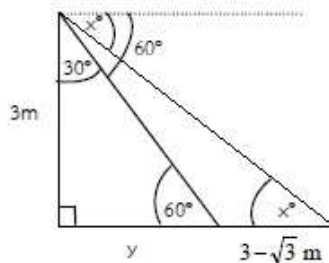
$$\text{ความยาวรอบรูปสามเหลี่ยม} = 2x + \sqrt{2}x$$

$$2 - \sqrt{2} = x(2 + \sqrt{2})$$

$$x = \frac{2 - \sqrt{2}}{2 + \sqrt{2}} = \frac{6 - 4\sqrt{2}}{2} = 3 - 2\sqrt{2}$$

$$\text{ด้านที่ยาวที่สุดยาว } (3 - 2\sqrt{2})\sqrt{2} = 3\sqrt{2} - 4 \text{ หน่วย}$$

16. 2



$$\tan 30^\circ = \frac{y}{3} \rightarrow \frac{1}{\sqrt{3}} = \frac{y}{3}$$

$$y = \frac{3}{\sqrt{3}} \rightarrow y = \sqrt{3}$$

ดังนั้น ระยะทางจากเสาตั้งกล้องถึงระยะทางที่กล้องจับภาพได้ไกลสุดยาว 3 เมตร จะได้ $x = 45^\circ$